ENGR 695 Advanced Topics in Engineering Mathematics Fall 2024

Selected Answers to HW #6

Provide the details of all solutions, including important intermediate steps. You will not receive credit for merely repeating an answer given here without supporting work.

If an answer is not provided below, it is either because the solution is trivial or because disclosure of the answer would reveal too much of the solution.

It is possible that one or more answers of the answers given below are incorrect because of the rush to post them. If you suspect that an answer is incorrect, please let me know as soon as possible.

1.
$$u_{i,j+1} = \frac{C^2}{1+\beta\Delta t}u_{i+1,j} + \frac{2(1-C^2)}{1+\beta\Delta t}u_{i,j} + \frac{C^2}{1+\beta\Delta t}u_{i-1,j} - \frac{1-\beta\Delta t}{1+\beta\Delta t}u_{i,j-1}$$
, where $C = \frac{v\Delta t}{\Delta x}$

2.
$$u_{i,n+1} = C^2 u_{i+1,n} + (2 - 2C^2) u_{i,n} + C^2 u_{i-1,n} - u_{i,n-1} - g\Delta t^2$$
, where $C = \frac{a\Delta t}{\Delta x}$

- **3.** [proof]
- **4.** [proof]